## 40 Bond <br> New York, NY

Technical Report 3


Samantha D'Agostino
Structural Option
Consultant - Dr. Thomas Boothby
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## Executive Summary

This third technical assignment includes an analysis and confirmation of the original lateral system designed by DeSimone Consulting Engineers (DCE). The loads calculated in the structural concepts and existing conditions report were applied to the lateral force resisting system composed of ordinary reinforced concrete shear walls. Necessary revisions were made to the initial wind and seismic loads, which were then included in the various load combinations set forth by ASCE 7-05 for strength design. An ETABS computer model was created and its output was compared to hand calculations to verify the shear strength of the system. Torsion, overturning and the impact on foundations were all examined in this manner. Overall building and story drifts were also compared to the allowable limits set forth by code and industry.

The computer model that was created included only the shear walls and the rigid diaphragms for the building. The gravity columns were not modeled at this stage in order to simplify this first attempt to create a model of 40 Bond. Also, hand calculations were done neglecting the presence of the coupling beams because of the involved nature of such calculations. There is acknowledgement, however, of how the coupling beams would affect certain results that were computed by hand.

After making such assumptions to complete the hand calculations, comparison were done between those values computed and those output from ETABS. It was determined that the model was taking the slab's rigidity into account and shifted the center of rigidity, while the calculations treated the shear walls as the only lateral force resisting elements. For this reason, the values computed by hand were those used in subsequent calculations including that for relative stiffness, torsion, direct shear, torsional shear, drift, displacement and overturning. The results suggest that it was reasonable to look only at the shear walls in this analysis. There were no serious concerns in regards to torsion, shear or overturning which suggests that the shear walls are providing the majority of the lateral resistance with minimal assistance from the slabs and none from the columns. Also, the drifts and displacement were within the limits and the values that seem somewhat large in size are attributed to the fact that the core was not examined as a core, but rather as individual shear walls acting independently.

## Introduction

40 Bond is located on a $13,600 \mathrm{ft}^{2}$ parcel of land located on Bond Street between Lafayette and Bowery Street in New York City. The footprint of the building is $64^{\prime}-8$ " by $134^{\prime}-4$ " and the building has an overall building height of $152^{\prime}-0$ " from the cellar to the top of the penthouse structure. There is a $20^{\prime}-0^{\prime \prime}$ setback at the seventh floor with a roof terrace that occupies this space. Typical spans range from $19^{\prime}-6^{\prime \prime} \times 25^{\prime}-0$ " to $23^{\prime}-2 \frac{1 / 2 "}{} \times 25^{\prime}-0$ " and floor-to-ceiling heights range from $11^{\prime}-10^{\prime \prime}$ to $14^{\prime}-0^{\prime \prime}$. A total of 23 condominium units and 5 townhouses are contained within this building and the plans vary as the type and number of units change throughout. In addition to the building there is also a 140 ' -0 " long, $22^{\prime}-0$ " high cast aluminum gate located along Bond Street that was designed to withstand the lateral forces that are present at this site.

## Architectural Design Concepts

40 Bond Street was designed by the Swiss firm Herzog \& de Meuron with New York based Handel Architects. The idea behind this luxury residential building was to reinvent the cast iron building typology that is prevalent in this lower Manhattan neighborhood. The building consists of one below grade level that houses a fitness center, storage space and equipment rooms. The first and second floors contain five through-building, 2-level townhouses. The layout then changes to accommodate four condominium units on each level from the third to the sixth floor. Once again, at the seventh floor the plans change incorporating a 20'-0" setback and reduced number of condominium units including only two per floor from levels 7 to 9 . The tenth floor is a full plan condominium with a penthouse structure that rises $20^{\prime}-0^{\prime \prime}$ above the main roof. In the penthouse a direct relation can be made between architectural concepts and structure. A 44’-0" clear span is achieved with two hidden columns and the core shear wall as supports leaving nearly three completely glass walls.

The south face also enforced some strict tolerances in regard to structure. Operable floor-to-ceiling windows are held in place with green glass mullions (Figure 1). This entirely glass façade limits the variation in columns to less than $1 / 2$ ". The north façade contains the same windows but the glass mullions are exchanged with pre-patina copper. These mullions then serve as a grid for the perimeter columns along the north and south faces. Small $10 " \times 10$ " concrete columns are located behind these mullions and space at $6^{\prime}-3$ " on center between the second and tenth floors. The variation in layout, fluctuating column dimensions, and necessary setbacks resulted in different transfer locations that required beams


Figure 1 - South Facade to redirect the loads.

With many buildings located in cities such as New York, there is always an awareness of retail value. The more space there is to offer the more expensive the unit may be. The flat plate concrete system allows for tall floor-to-ceiling heights that remain unobstructed because of the limited number of beams and girders dropping into the space. In order to preserve the architectural design, maximize area and create appealing spaces, the concrete structure deviates from what is typical in the design and construction of a residential building to create an aesthetically pleasing and interesting structure. As a result of these characteristics, however, this $90,000 \mathrm{sf}$ building had a very high cost in comparison to its size which is attributed to such things as formwork required for transfer beams and many slender columns.

## Structural System

## Foundation

The geotechnical engineering study was performed by Langan Engineering \& Environmental Services on September 10, 2004. In this study it was found that the water level was approximately 42.8 ' below the existing ground surface. The cellar extends 12 '- 8 " below grade and therefore there was not a concern in regard to increased uplift pressures at this level. Langan noted that the bearing materials were suitable for a shallow foundation and that the recommended allowable bearing pressure would be $5 \mathrm{kips} / \mathrm{ft}^{2}$. As a result, a 30 " reinforced concrete mat foundation was designed with bearing walls and buttresses supported by a strip footing.

The 30" slab is 5 ksi normal weight concrete (NWC) and increases to a thickness of 48" and 84" within the core shear walls where the elevator pit is located. Reinforcement varies throughout this mat slab. Buttresses ranging in size from $14 " \times 291 / 2$ " to $18 " \times 79$ " are located around the perimeter. Interior columns ranging in size from $12 " \times 22^{\prime \prime}$ to $28^{\prime \prime} \times 28^{\prime \prime}$ have an increased strength of 8 ksi . Located at columns 3B, 3C and 3F (Figure 2), there are also foundation mat shearheads to resist punching shear due to high loads that continue from the roof down to the foundation.


Figure 2 - Foundation Plan with Typical Column Grid and Shearhead Locations Noted

## Superstructure

The ground floor is a 9" two-way flat plate (NWC) with a compressive strength ( $\mathrm{f}^{\prime}$ c) of 5.95 ksi and typical reinforcement of \#4@12 top and bottom with various sizes and spacing of bars at column locations. Located at the south face is a slab step that transitions to a 12 " slab for the townhouse entrances. Typical to the floors above, there are also 3" slab depressions at the fireplaces and toilet areas and 14 " slabs within the core. Perimeter columns ranging in size from $10 " \times 24$ " to $16 " \times 58$ " are located on the north, south and east walls while a 12 " thick shear wall runs along the west face. The interior columns dimensions are then $12 " \times 22$ ", 22 " $\times 22^{\prime \prime}$ and 28 "x28". All of the columns from the foundation to those supporting the fourth floor have a concrete strength of 8 ksi . There are beams located around the stair openings in the townhouses and coupling beams that tie together the core shear walls which are typical on all floors.

The second and third floors have the same two-way flat plate slab as above without the slab step. Particular to the second floor is the introduction of the 10 " $\times 10^{\prime \prime}$ concrete columns spaced at 6 ' -3 " on center along the north wall that extend up the remaining height of the building. Because these closely spaced columns need to transition to fewer columns below, 14 " $\times 40$ " transfer beams ( $\mathrm{f}_{\mathrm{c}}{ }^{\prime}=$ 10 ksi , typical to all transfer beams) run the full length of this wall. The beams around the townhouse stair openings are also present on the second floor. The third floor then has the introduction of the 10 " $\times 10^{\prime \prime}$ columns spaced at 6 ' -3 " on center along the south face. The transfer
beams at this level are $60 " \times 16^{\prime \prime}$ and extend the full length of this wall. These columns continue to the seventh floor where they step back 20'-0" due the setback at that level. This thin, wide transfer was implemented to limit the intrusion into the space below. Also, all the 10 " $\times 10$ " columns only have a 7 " slab encroachment that has a 1" slab depression around each column (Figure 3).

All floors between level 4 to the penthouse level use a 9" two-way flat plate with \#4@12 top and


Figure 3 - Typical Perimeter Column Detail bottom plus various reinforcement at columns and a reduced compressive strength of $\mathrm{f}^{\prime}{ }_{\mathrm{c}}=5 \mathrm{ksi}$. Similar slab depressions and increased slab thickness at the core are present. The columns supporting the fifth floor and above also have a lower compressive strength of $\mathrm{f}^{\prime}{ }_{\mathrm{c}}=5 \mathrm{ksi}$. The columns along the north and south façade remain 10 " $\times 10$ " while those located on the east and west walls and within the interior vary between $12 " \times 22$ " to 28 " $\times 28$ ". There is also the introduction of 22 " diameter ( $\varnothing$ ) circular columns that are used on some floors dependent on the tenant's request in their condominium. In addition to the beams within the shear wall core, there are also spandrel beams along the east and west faces.

At the fourth floor a transfer beam is present along the east wall (Figure 4). This 12 " $\times 50$ " transfer was designed after construction began due to the presence of an adjacent chimney encroachment on site. Then at the seventh floor the setback takes place. It is here that loads increase due to the roof terrace provided by this setback. A 20 " $\times 24$ " transfer beam along line 2 is needed, due to the introduction of the 10 " $\times 10$ " columns along this line (Figure 5 ).


Figure 4 - Transfer Beam at Fourth Floor


Figure 5 - Transfer Beam at Seventh Floor

The penthouse level and its roof are a great example of what can be achieved when using concrete. The dimensions of the penthouse are $23^{\prime}-4 " \times 44^{\prime}-6$ " and it has a thickened 19 " slab with \#4@12 top bar reinforcement and \#5@8 bottom bar reinforcement. A 44’-0" clear span is
achieved with the support of the concrete shear walls to the east and two 28 " $\times 16$ " columns to the west. The loads from the two columns need to be transferred and a 32 " $\times 24$ " beam is used to direct these loads to nearby columns, one of which is only $10 " \times 14$ ". The roof above this long span structure is a combination of upturned beams, inclined piers, and two separate 8" slabs with \#5@12 top and bottom spanning between its two supports (Figure 6). Located on the other side of the core is an enclosed elevated mechanical room. Additional loads due to the


Figure 6 -Penthouse Roof Structure equipment and its surrounding 8 " CMU walls will be applied at this level.

## Lateral System

The lateral system is a combination of 12" ordinary reinforced concrete shear walls (Figure 7). Elevations of these walls are located in Appendix A, which clearly defines all openings and the location of coupling beams throughout the height of the building. The typical horizontal reinforcement in these walls is \#4@12 while the vertical reinforcement ranges from \#4@12 to \#8@6 depending on the level they are located on and which portion of the shear wall is being examined. The west shear wall is reinforced with \#4@12 as the horizontal reinforcement and a range of vertical reinforcement from \#4@12 to \#7@12. All shear walls supporting the ground


Figure 7 - Typical Plan with Lateral System Highlighted
floor to those supporting the fourth floor have concrete with a compressive strength $\mathrm{f}^{\prime}{ }_{\mathrm{C}}=8 \mathrm{ksi}$ while those supporting the rest of the building have an $\mathrm{f}^{\prime}{ }_{\mathrm{c}}=5 \mathrm{ksi}$.

The presence of the west shear wall allows for the center of rigidity to move closer towards the middle of the plan. Because the core shear walls are not centralized within the building they draw the rigidity to the east. When the center of rigidity is not in line with the resultant lateral force there is eccentricity and moments due to torsion become a factor.

## Loads

## Gravity Loads

The determination of gravity loads by DCE was done using the New York City Building Code (NYCBC 2003), while American Society of Civil Engineers (ASCE) 7-05 was the main reference for this report. A different standard was used to comply with the requirements of AE Senior Thesis; ASCE 7-05 was the logical reference. Another note is that DCE chooses not to use live load reductions in their design. In order to keep the loading consistent, the reductions will be not be factored into the live loads determined by code. The loads that were determined from each reference as well as the design loads are noted in Table 1.

| Table 1 - Gravity Loads |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Description | NYCBC (2003) | ASCE 7-05 | DCE Value | Design Value |
| DEAD (DL) |  |  |  |  |
| Concrete | 150 pcf | 150 pcf | 150 pcf | 150 pcf |
| LIVE (LL) |  |  |  |  |
| Condominiums \& Townhouses | 40 psf | 40 psf | 40 psf | 40 psf |
| Corridor (first floor, main lobby) | 100 psf | 100 psf | 100 psf | 100 psf |
| Corridor (serving independent units) | 40 psf | 40 psf | 40 psf | 40 psf |
| *Exterior Balconies | 60 psf | 100 psf | 60 psf | 100 psf |
| SUPERIMPOSED (SDL) |  |  |  |  |
| Finishes, MEP, Partitions | 20-25 psf | 20-25 psf | 20 psf | 25 psf |
| **Concrete Pavers | 40 psf | 40 psf | 40 psf | 40 psf |
| SNOW (S) |  |  |  |  |
| ***Snow | 30 psf | 21 psf | 30 psf | 30 psf |
| * In NYCBC, exterior balcony LL is $150 \%$ of adjacent areas. Therefore $(40 \mathrm{psf}) \times(1.5)=60 \mathrm{psf}$. |  |  |  |  |

## Wind Loads

Wind loads were determined using ASCE 7-05 Section 6.5 which describes Method 2-Analytical Procedure. The variables used in this analysis are located in Table 2 and these values are supported by base calculations located in Appendix B. The wind analysis done for this technical assignment varies from that done by DCE because of their use of the NYCBC. Rather than calculating the pressures at each floor, a simplified diagram found in the code was used that relates three distinct pressures at three distinct heights (Figure 8).


Figure 8 - Wind Load Diagram from NYCBC - RS 9-5

| Table 2 - Wind Variables |  |  | (ASCE <br> References) |
| :---: | :---: | :---: | :---: |
| Basic Wind Speed | V | 110 mph | (Fig. 6-1) |
| Directionality Factor | $\mathrm{k}_{\text {d }}$ | 0.85 | (Table 6-4) |
| Importance Factor | I | 1.00 | (Table 6-1) |
| Exposure Category |  | B | (Sec. 6.5.6.3) |
| Topographic Factor | $\mathrm{K}_{\text {zt }}$ | 1.00 | (Sec. 6.5.7.1) |
| Velocity Pressure Exposure Coefficient evaluated at Height z | $\mathrm{K}_{\mathrm{z}}$ | Varies | (Table 6-3) |
| Velocity Pressure at Height z | $\mathrm{q}_{\mathrm{z}}$ | Varies | (Eq. 6-15) |
| Velocity Pressure at Mean Roof Height | $\mathrm{q}_{\mathrm{h}}$ | 27.909 | (Eq. 6-15) |
| Equivalent Height of Structure | > | 76.14' | (Table 6-2) |
| Intensity of Turbulence | I> | 0.261 | (Eq. 6-5) |
| Integral Length Scale of Turbulence | L, | 422.8' | (Eq. 6-7) |
| Background Response Factor (East/West) | Q | 0.85 | (Eq. 6-6) |
| Background Response Factor (North/South) | Q | 0.826 | (Eq. 6-6) |
| Gust Effect Factor (East/West) | G | 0.9097 | (Eq. 6-4) |
| Gust Effect Factor (North/South) | G | 0.828 | (Eq. 6-4) |
| External Pressure Coefficient (Windward) | $\mathrm{C}_{\mathrm{p}}$ | 0.8 | (Fig. 6-6) |
| External Pressure Coefficient (E/W <br> Leeward) | $\mathrm{C}_{\mathrm{p}}$ | -0.3 | (Fig. 6-6) |
| External Pressure Coefficient (N/S <br> Leeward) | Ср | -0.5 | (Fig. 6-6) |

Tables and calculations supporting the wind pressures in the both directions are also located in Appendix B. The winds coming in the north/south direction are those most prevalent at the site because two adjacent buildings are located on both the east and west sides of 40 Bond. The summation of windward story shear calculated by ASCE 7-05 is within 10 kips of that found by DCE, which insinuates that although there was a variation in pressures used, both methods provide reasonable answers and therefore either method can be used interchangeably. The reason behind these calculations being lower can be due to the fact that my windward pressures never exceed 25 psf and go below the lower limit of 20 psf provided by the NYCBC.

Although there are currently adjacent buildings blocking the wind on the lower levels, wind in the east/west direction must be examined in the event that these structures are absent at some point in the future and the full wind load is applied. The summation of windward story shear calculated by ASCE 7-05 is within 5 kips of that found by DCE. Similar conclusions to those stated for the north/south pressures can be applied here.

## Seismic Loads

In order to calculate the seismic forces on 40 Bond, Chapters 11 and 12 were referenced from ASCE 7-05. DCE performed the seismic analysis based on the NYCBC, and there is a large difference between the base shears. After speaking with faculty in the Architectural Engineering department it was noted that such a great difference in possible when working between two separate codes/standards.

An assumption that was made in this analysis was that 40 Bond employed a rigid diaphragm which allowed for the use of the Equivalent Lateral Force Procedure found in Section 12.8 within ASCE 7-05. The variables used in this procedure are located in Table 3. The story shear, using these variables is then computed as,

$$
V=C_{s} W
$$

with W being the effective seismic weight as per Section 12.7.2.

| Table 3 - Seismic Design Variables |  |  | (ASCE Reference) |
| :---: | :---: | :---: | :---: |
| Soil Classification |  | B | (Table 20.3-1) |
| Occupancy |  | II | (Table 1-1) |
| Importance Factor |  | 1.00 | (Table 11.5-1) |
| Structural System |  | Building Frame System: Ordinary Reinforced Concrete Shear Wall | (Table 12.2-1) |
| Spectral Response Acceleration, short | $\mathrm{S}_{\text {s }}$ | 0.361 | (USGS) |
| Spectral Response Acceleration, 1 s | $\mathrm{S}_{1}$ | 0.07 | (USGS) |
| Site Coefficient | $\mathrm{F}_{\mathrm{a}}$ | 1.00 | (Table 11.4-1) |
| Site Coefficient | $\mathrm{F}_{\mathrm{v}}$ | 1.00 | (Table 11.4-2) |
| MCE Spectral Response Acceleration, short | $\mathrm{S}_{\mathrm{MS}}$ | 0.361 | (Eq. 11.4-1) |
| MCE Spectral Response Acceleration, 1 s | $\mathrm{S}_{\mathrm{M} 1}$ | 0.07 | (Eq. 11.4-2) |
| Design Spectral Acceleration, short | $\mathrm{S}_{\mathrm{DS}}$ | 0.241 | (Eq. 11.4-3) |
| Design Spectral Acceleration, 1 s | $\mathrm{S}_{\mathrm{D} 1}$ | 0.047 | (Eq. 11.4-4) |
| Seismic Design Category | $\mathrm{S}_{\mathrm{DC}}$ | B | (Table 11.6-2) |
| Response Modification Coefficient | R | 5 | (Table 12.2-1) |
| Approximate Period Parameter | $\mathrm{C}_{\mathrm{t}}$ | 0.02 | (Table 12.8-2) |
| Building Height (above grade) | $\mathrm{h}_{\mathrm{n}}$ | 134.3 ft | Above Grade |
| Approximate Period Parameter | X | 0.75 | (Table 12.8-2) |
| Calculated Period Upper Limit Coefficient | $\mathrm{C}_{\mathrm{u}}$ | 1.70 | (Table 12.8-1) |
| Approximate Fundamental Period | Ta | 0.789 s | (Eq. 12.8-7) |
| Fundamental Period | T | 1.34 s | (Sec. 12.8.2) |
| Long Period Transition Period | $\mathrm{T}_{\mathrm{L}}$ | 6.00 s | (Fig. 22-15) |
| Seismic Response Coefficient | $\mathrm{C}_{\text {s }}$ | 0.012 | (Eq. 12.8-2) |
| Structure Period Exponent | k | 1.42 | (Sec. 12.8.3) |

The NYCBC makes use of different variables and equations in comparison to ASCE 7-05. In most cases it was clear that certain variables were directly related to the other and the only difference being in the coefficients used to describe them. An example of this was Site Class $\mathrm{S}_{1}$ in the NYCBC which referred to materials with shear wave velocity greater than $2500 \mathrm{ft} / \mathrm{s}$. This same description was used for Site Class B within ASCE 7-05. There were also instances were coefficients were not comparable, such as the response modification factor. In the NYCBC, $\mathrm{R}_{\mathrm{w}}=8$ for ordinary reinforced concrete shear walls within the building frame system, while $\mathrm{R}=5$ in ASCE 7-05. The variables needed to calculate base shear according to the building code are located in Table 4. The calculation for base shear according to the NYCBC is,

$$
V=\frac{Z I C}{R_{W}} W
$$

with W equal to the effective building weight.

| Table 4 - Seismic Design Variables |  | (NYCBC Reference) |  |
| :--- | :---: | :--- | :---: |
| Seismic Zone Factor | Z | 0.15 | (RS 9-6) |
| Importance Factor | I | 1 | (RS 9-6) |
| Site Coefficient for $\mathrm{S}_{1}$ Soil | S | 1.00 | (RS 9-6) |
| Response Modification Coefficient | $\mathrm{R}_{\mathrm{w}}$ | 8.00 | (RS 9-6) |
| Overall Building Height | hn | 152 | Above and Below Grade |
| Coefficient | C | 1.47 | (RS 10-5c) |

To adhere to the requirement of using ASCE 7-05, the story shears and overturning were calculated using this standard. To ensure, however, that the most stringent loads were accounted for, calculations were also done according to the NYCBC. These values were then used for the analysis and confirmation design of the lateral system required in this technical assignment. All supporting calculations and tables are located in Appendix B.

## ETABS Model

ETABS is a computer modeling and analysis program developed by Computers \& Structures, Inc. For the use in this technical assignment, the building's lateral system and diaphragms were the only components modeled (Figure 9). This simplification required the gravity loads to be applied as additional area masses to the diaphragms. The mass of each of the shear walls was incorporated into membranes that defined each portion of the wall. These walls were meshed into areas with a maximum dimension of $24 " \times 24$ " that allowed those walls that were connected at the core to act together as a rigid unit. Also, for simplicity, the coupling beams were modeled as wall elements as opposed to line elements. The results from this model were compared to the values produced by hand calculations of the center of mass, center of rigidity, and story displacements. Additional information to the overall building drift and controlling load cases were also pulled from the model.


Figure 9 - ETABS Computer Model

## Load Considerations

## Load Combinations

The list below shows the various load cases specified by ASCE 7-05 Section 2.3 for factored loads using strength design.

$$
\begin{aligned}
& 1.4(D+F) \\
& 1.2(D+F+T)+1.6(L+H)+0.5\left(L_{r} \text { or } S \text { or } R\right) \\
& 1.2 D+1.6\left(L_{r} \text { or } S \text { or } R\right)+(L \text { or } 0.8 W) \\
& 1.2 D+1.6 W+L+0.5\left(L_{r} \text { or } S \text { or } R\right) \\
& 1.2 D+1.0 E+L+0.2 S \\
& 0.9 D+1.6 W+1.6 H \\
& 0.9 D+1.0 E+1.6 H
\end{aligned}
$$

These combinations were included in the ETABS model and after looking into drift, story shears and displacements it was determined that the controlling load case in the north/south direction was $1.2 D+1.6 W+L+0.5\left(L_{r}\right.$ or $S$ or $\left.R\right)$ and in the east/west direction $0.9 D+1.0 E+1.6 H$. The wind in the north/south direction controls because of the large surface area along that face, which produces higher forces. The east and west facades are less than half the surface area seen on the north and south faces so it seems quite reasonable that seismic controls in that direction.

## Load Path and Distribution

As the lateral forces come in contact with the building, the loads need a means of travelling through the structure and into the ground. The load path is assumed to be controlled by the concept of relative stiffness. Those members that are the most rigid draw the forces to them. As a result the loads are transmitted through the diaphragms, to the shear walls, and then down into the mat foundation. After completing this assignment, it is clear that the shear walls with minimal assistance from the slabs resist the lateral forces, while the columns only serve to transmit gravity loads.

40 Bond has a shear wall located along the west face of the building in addition to a shear wall core. Figure 10 shows the numbered system assigned to each wall to better reference exactly which shear walls are being discussed throughout this paper. Although all the shear walls maintain the same thickness of 12 " throughout their heights, they do vary in length and are located different distances from the center of rigidity of the building. These things all affect the rigidity of the walls which in turn affects the relative stiffness of each element. Tables located in Appendix C define the rigidities of Walls 1-3 (parallel to the north/south lateral forces) and of


Figure 10 - Numbered Shear Walls
Walls 4-7 (parallel to the east/west lateral forces) that were calculated using the following equation:

$$
R=\frac{E t}{4\left(\frac{h}{L}\right)^{3}+3\left(\frac{h}{L}\right)}
$$

The rigidity values were then used to determine the center of rigidity on each floor which can be calculated as:

$$
\text { Center of Rigidity }=\frac{\Sigma(R)(\text { distance between element and the origin })}{\Sigma R}
$$

The values of both the center of mass and center of rigidity are located in Table 5. The coordinates found by hand calculations and the ETABS output are put in this one table to show that the results are comparable. The center of rigidity values taken from the ETABS model suggest that the diaphragms are being considered in the determination of rigidity, as opposed to the hand calculations that are assuming that only the shear walls are to be taken into account.
For the use in this technical assignment, the values produced by hand calculations will be those used whenever the center of mass and center of rigidity are needed.

| Table 5 |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Center of Rigidity |  |  |  | Center of Mass |  |  |  |
|  | Etabs Output |  | Hand Calculations |  | Etabs Output |  | Hand Calculations |  |
|  | X | Y | X | Y | X | Y | X | Y |
| Floor 2 | - | - | 706.3633 | 642.197 | 800 | 376.250 | 800 | 376.25 |
| Floor 3 | 765.475 | 637.376 | 730.124 | 566.123 | 800.000 | 376.250 | 800 | 376.25 |
| Floor 4 | 803.596 | 580.913 | 744.207 | 550.703 | 800.000 | 376.250 | 800 | 376.25 |
| Floor 5 | 823.685 | 567.171 | 751.278 | 543.547 | 800.000 | 376.250 | 800 | 376.25 |
| Floor 6 | 835.359 | 561.839 | 755.113 | 539.356 | 800.000 | 376.250 | 800 | 376.25 |
| Floor 7 | 843.340 | 559.478 | 757.485 | 536.020 | 800.000 | 376.250 | 800 | 376.25 |
| Floor 8 | 848.189 | 559.509 | 800.786 | 535.059 | 800.000 | 496.250 | 800 | 496.25 |
| Floor 9 | 853.058 | 560.267 | 833.890 | 534.052 | 800.000 | 496.250 | 800 | 496.25 |
| Floor 10 | 858.271 | 561.266 | 857.899 | 533.013 | 800.000 | 496.250 | 800 | 496.25 |
| Penthouse | 864.205 | 561.852 | 876.731 | 530.580 | 800.000 | 496.250 | 800 | 496.25 |
| Penthouse Roof | 882.870 | 608.262 | 951.500 | 655.000 | 865.000 | 521.500 | 865 | 521.50 |

The rigidity of the walls is also used to determine the relative stiffness, which dictates what percentage of the lateral force is distributed it each wall. This is simply calculated as:

$$
\text { Relative Stiffness }=\frac{R}{\Sigma R}
$$

Table 6 gives the values found for all seven walls at every level. These values can then be directly applied to the loads at each floor to determine how much each wall will receive. Also, it is important to note that because the length of the walls change as they continue up the building, either due to setbacks or the addition of openings, the relative stiffness of one wall is not consistent its entire height. As the contribution of each wall changes, so does the relative stiffness of each member resisting the force in the specified direction.

| Table 6 - Relative Stiffness (\%) |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Wall 1 | Wall 2 | Wall 3 | Wall 4 | Wall 5 | Wall 6 | Wall 7 |
|  | 25.93 | 37.04 | 37.04 | 64.90 | 31.14 | 0.09 | 3.87 |
| Floor 1 | 23.41 | 38.29 | 38.29 | 50.60 | 21.88 | 20.20 | 7.32 |
| Floor 2 | 21.92 | 39.04 | 39.04 | 47.71 | 20.00 | 21.67 | 10.62 |
| Floor 3 | 21.18 | 39.41 | 39.41 | 46.30 | 19.19 | 22.16 | 12.35 |
| Floor 4 | 20.77 | 39.61 | 39.61 | 45.46 | 18.74 | 22.33 | 13.47 |
| Floor 5 | 20.52 | 39.74 | 39.74 | 44.77 | 18.40 | 22.63 | 14.21 |
| Floor 6 | 15.94 | 42.03 | 42.03 | 44.58 | 18.29 | 22.50 | 14.64 |
| Floor 7 | 12.44 | 43.78 | 43.78 | 44.37 | 18.18 | 22.37 | 15.07 |
| Floor 8 | 9.90 | 45.05 | 45.05 | 44.15 | 18.08 | 22.25 | 15.52 |
| Floor 9 | 7.91 | 46.05 | 46.05 | 43.63 | 17.85 | 22.66 | 15.86 |
| Floor 10 | Penthouse | 0.00 | 50.00 | 50.00 | 0.00 | 100.00 | 0.00 |

## Torsion

Torsion is present when the center of mass and the center of rigidity are not in the same location. Moments are produced by this eccentricity and torsional shear becomes an additional force to account for. Torsional shear will be discussed further when shear is reviewed.

There are two separate moments to take into consideration when looking at torsion in buildings with rigid diaphragms, like those seen in 40 Bond, according to ASCE 7-05 Section 12.8.4. First there is the inherent moment, $\mathrm{M}_{\mathrm{t}}$, which is due to eccentricity between the center of rigidity and the center of mass. Because of the rigidity of the slab there is also an accidental moment, $\mathrm{M}_{\mathrm{t}}$, which needs to be accounted for in addition to the inherent moment. This moment is "caused by the assumed displacement of the center of mass each way from the actual location by a distance equal to $5 \%$ of the dimension of the structure perpendicular to the direction of the applied force." The values of the torsion, produced by forces in both directions, can be seen in Table 7.

| Table 7 - Overall Building Torsion |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | North/South Direction |  |  |  | East/West Direction |  |  |  |
|  | Factored Lateral Force (k) | $\begin{gathered} \mathrm{M}_{\mathrm{t}} \\ (\mathrm{ft}-\mathrm{k}) \end{gathered}$ | $\begin{gathered} \mathrm{M}_{\mathrm{ta}} \\ (\mathrm{ft}-\mathrm{k}) \end{gathered}$ | $\begin{aligned} & \mathrm{M}_{\mathrm{t}, \mathrm{tot}} \\ & (\mathrm{ft}-\mathrm{k}) \end{aligned}$ | Factored Lateral Force (k) | $\begin{gathered} \mathrm{M}_{\mathrm{t}} \\ (\mathrm{ft}-\mathrm{k}) \end{gathered}$ | $\begin{gathered} \mathrm{M}_{\mathrm{ta}} \\ (\mathrm{ft}-\mathrm{k}) \end{gathered}$ | $\begin{aligned} & \mathrm{M}_{\mathrm{t}, \mathrm{tot}} \\ & (\mathrm{ft}-\mathrm{k}) \end{aligned}$ |
| Floor 2 | 91.13 | -711.09 | 607.38 | -103.71 | 25.23 | 6710.65 | 79.17 | 6789.82 |
| Floor 3 | 108.12 | -629.59 | 720.63 | 91.04 | 64.11 | 12172.57 | 201.14 | 12373.71 |
| Floor 4 | 99.70 | -463.56 | 664.52 | 200.96 | 45.37 | 7914.97 | 142.35 | 8057.32 |
| Floor 5 | 98.37 | -399.41 | 655.66 | 256.24 | 39.52 | 6611.39 | 123.99 | 6735.38 |
| Floor 6 | 96.60 | -361.34 | 643.83 | 282.50 | 33.96 | 5539.57 | 106.56 | 5646.13 |
| Floor 7 | 100.84 | -357.26 | 672.08 | 314.82 | 42.67 | 6816.82 | 133.87 | 6950.69 |
| Floor 8 | 92.61 | 6.06 | 617.23 | 623.30 | 33.13 | 1285.88 | 103.96 | 1389.84 |
| Floor 9 | 89.95 | 254.02 | 599.50 | 853.52 | 25.52 | 964.52 | 80.05 | 1044.57 |
| Floor 10 | 87.29 | 421.15 | 581.77 | 1002.91 | 18.48 | 679.55 | 58.00 | 737.54 |
| Penthouse | 76.66 | 490.19 | 510.94 | 1001.13 | 12.63 | 433.74 | 39.64 | 473.39 |
| Penthouse Roof | 84.73 | 610.79 | 564.75 | 1175.53 | 5.54 | 739.09 | 17.37 | 756.46 |
|  |  |  | Total | 5698.25 |  |  | Total | 50954.85 |

## Shear

## Direct Shear

Direct shear is that which is caused by the lateral forces acting on a building that are distributed to the shear walls. To determine these values simply multiply the story shear by the relative stiffness of each member. The direct shears that will be applied to each wall can be found in Tables 8 and 9.

| Table 8 - North/South Direct Shear |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Load Combination <br> 1.2D + 1.6L + L + 0.5Lr | Force (k) | Factored <br> Force (k) | Distributed Force (k) |  |  |
| Floor 2 |  |  |  | Wall 2 | Wall 3 |
| Floor 3 | 56.96 | 91.13 | 23.63 | 33.75 | 33.75 |
| Floor 4 | 67.58 | 108.12 | 25.32 | 41.40 | 41.40 |
| Floor 5 | 62.31 | 99.70 | 21.86 | 38.92 | 38.92 |
| Floor 6 | 61.48 | 98.37 | 20.83 | 38.77 | 38.77 |
| Floor 7 | 60.37 | 96.60 | 20.06 | 38.27 | 38.27 |
| Floor 8 | 63.02 | 100.84 | 20.69 | 40.07 | 40.07 |
| Floor 9 | 57.88 | 92.61 | 14.76 | 38.92 | 38.92 |
| Floor 10 | 56.22 | 89.95 | 11.19 | 39.38 | 39.38 |
| Penthouse | 54.55 | 87.29 | 8.64 | 39.32 | 39.32 |
| Penthouse Roof | 47.91 | 76.66 | 6.06 | 35.30 | 35.30 |


| Table 9 - East/ West Direct Shear |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Load Combination <br> 0.9D + 1.0E + 1.6H | Force (k) | Factored <br> Force (k) | Wall 4 | Wall 5 | Wall 6 | Wall 7 |
| Floor 2 |  |  |  | Distributed Forces (k) |  |  |
| Floor 3 | 25.23 | 25.23 | 16.38 | 7.86 | 0.02 | 0.98 |
| Floor 4 | 64.11 | 64.11 | 32.44 | 14.03 | 12.95 | 4.69 |
| Floor 5 | 45.37 | 45.37 | 21.64 | 9.08 | 9.83 | 4.82 |
| Floor 6 | 39.52 | 39.52 | 18.30 | 7.58 | 8.76 | 4.88 |
| Floor 7 | 33.96 | 33.96 | 15.44 | 6.36 | 7.59 | 4.57 |
| Floor 8 | 42.67 | 42.67 | 19.10 | 7.85 | 9.65 | 6.06 |
| Floor 9 | 33.13 | 33.13 | 14.77 | 6.06 | 7.45 | 4.85 |
| Floor 10 | 25.52 | 25.52 | 11.32 | 4.64 | 5.71 | 3.85 |
| Penthouse | 18.48 | 18.48 | 8.16 | 3.34 | 4.11 | 2.87 |
| Penthouse Roof | 12.63 | 12.63 | 5.51 | 2.26 | 2.86 | 2.00 |

## Torsional Shear

In addition to direct shear there is also a shear force present when torsion is produced by the building. To determine this value the following equation was used:

$$
T=\frac{V_{t o t} e d_{i} R_{i}}{J}
$$

- $\mathrm{V}_{\text {tot }}=$ story shear
- $e=$ distance from the center of mass to the center of rigidity
- $\mathrm{d}_{\mathrm{i}}=$ distance from element to the center of rigidity
- $\mathrm{R}_{\mathrm{i}}=$ relative stiffness of the element
- $\mathrm{J}=$ torsional moment of inertia $=\Sigma \Sigma\left(R \times d_{i}{ }^{2}\right)$

As an example, the torsional shear was computed for the shear wall supporting Floor 6 and can be found in Table 10.

| Table 10 - Torsional Shear in Shear Wall Supporting Floor 6 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Factored Story Shear $\mathrm{V}_{\text {tot }}(\mathrm{k})$ | Relative Stiffness $\mathrm{R}_{\mathrm{i}}$ | Distance from COM to COR e (inches) | Distance from Wall X to COR $\mathrm{d}_{\mathrm{i}}$ (inches) | $\left(\mathrm{R}_{\mathrm{i}}\right)\left(\mathrm{d}_{\mathrm{i}}^{2}\right)$ | Torsional Shear (k) |
| Wall 1 | N/S | 687.38 | 0.208 | 44.89 | 749.11 | 116555.07 | 25.76 |
| Wall 2 | N/S | 687.38 | 0.396 | 44.89 | 57.39 | 1304.46 | 3.76 |
| Wall 3 | N/S | 687.38 | 0.396 | 44.89 | 335.39 | 44555.08 | 21.99 |
| Wall 4 | E/W | 250.86 | 0.455 | 163.11 | 115.64 | 6079.62 | 11.54 |
| Wall 5 | E/W | 250.86 | 0.187 | 163.11 | 115.64 | 2506.21 | 4.76 |
| Wall 6 | E/W | 250.86 | 0.223 | 163.11 | 207.36 | 9601.11 | 10.16 |
| Wall 7 | E/W | 250.86 | 0.135 | 163.11 | 207.36 | 5791.62 | 6.13 |
| Torsional Moment of Inertia $\mathrm{J}=\Sigma\left(\mathrm{R}_{\mathrm{i}}\right)\left(\mathrm{d}_{\mathrm{i}}^{2}\right)=$ |  |  |  |  |  | 186393.18 |  |

## Shear Strength Check

In order to confirm the shear strength of the shear walls, a check must be done that takes into account both the torsional and direct shears being applied. According to ACI 318-08 Section 21.9.4.1 the shear strength of a reinforced concrete shear walls is defined as:

$$
V_{n}=A_{c v}\left[\left(\alpha_{c} \lambda \sqrt{f^{\prime}}{ }_{c}\right)+\left(\rho_{t} f_{y}\right)\right]
$$

The hand calculations of a strength check done at the shear walls supporting Floor 6 can be found in Appendix D. Each wall was well within the capacity determined with the above
equations which can be seen in Table 11. The original shear wall details that were used to confirm the reinforcement and spacing are seen in Figure 11.

| Table 11 - Shear Wall Strength Check (Supporting Floor 6) |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Floor 6 | Direct Shear (k) | Torsional Shear (k) | $\mathrm{V}_{\mathrm{u}}(\mathrm{k})$ | Vertical <br> Reinf. | Spacing <br> (in) | Length <br> (in) | Thickness (in) | $\mathrm{A}_{\mathrm{cv}}\left(\mathrm{in}{ }^{2}\right)$ | $\alpha_{\text {c }}$ | $\rho_{\text {t }}$ | $\phi \mathrm{V}_{\mathrm{n}}(\mathrm{k})$ |  |
| Wall 1 | 81.41 | 25.76 | 107.17 | (2) \#6 | 12 | 256 | 12 | 3072 | 2 | 0.0061 | 1170.63 | OK |
| Wall 2 | 273.63 | 3.76 | 277.39 | (2) \#5 | 12 | 323 | 12 | 3876 | 2 | 0.0043 | 1162.08 | OK |
| Wall 3 | 273.63 | 21.99 | 295.62 | (2) \#4 | 12 | 323 | 12 | 3876 | 2 | 0.0028 | 895.61 | OK |
| Wall 4 | 74.31 | 11.54 | 85.85 | (2) \#6 | 12 | 122 | 12 | 1464 | 2 | 0.0061 | 557.88 | OK |
| Wall 5 | 36.05 | 4.76 | 40.80 | (2) \#5 | 8 | 90.5 | 12 | 1086 | 2 | 0.0065 | 430.81 | OK |
| Wall 6 | 37.38 | 10.16 | 47.54 | (2) \#5 | 12 | 99 | 12 | 1188 | 2 | 0.0043 | 356.18 | OK |
| Wall 7 | 24.21 | 6.13 | 30.34 | (2) \#5 | 8 | 90.5 | 12 | 1086 | 2 | 0.0065 | 430.81 | OK |



Figure 11 - Details of shear wall supporting Floor 6

## Drift and Displacement

Drift is a serviceability consideration in building design that in inversely proportionate to rigidity. The overall building drift should be limited as much as possible, especially in the case of 40 Bond, because the building is attached to adjacent buildings on either side. The drift has been limited to $1 / 400^{\text {th }}$ of the overall building height which originated from the Structural Engineering Handbook (1968) by Gaylord and Gaylord. In the case of 40 Bond, the drift limit is:

$$
\Delta_{\text {limit }}=\left(1612^{\prime \prime} / 400\right)=4.03^{\prime \prime}
$$

The building drifts taken from the ETABS model describe a drift in the x-direction (due to east/west forces) $=1.1422$ " which is well below 4.03". Similarly, the drift in the $y$-direction (due to north/south forces) $=1.0474$ " is within the limits enforced.

Each floor can be examined independently to obtain an approximate determination of the displacements and story drifts. This was done by hand calculations using the following equation:

$$
\Delta_{\text {cantilever }}=\Delta_{\text {flexural }}+\Delta_{\text {shear }}=\frac{P h^{3}}{3 E_{c} I}+\frac{1.2 P h}{E_{r} A}
$$

The actual calculations as well as tables looking at the story drift and displacement of Walls 1-3 can be found in Appendix E. Note that the modulus of elasticity and the modulus of rigidity change values once the shear wall supporting Floor 5 is examined. The reason for this is because the concrete strength is $\mathrm{f}^{\prime}{ }_{\mathrm{c}}=8000 \mathrm{psi}$ for the walls supporting Floors $1-4$ and then $\mathrm{f}^{\prime}{ }_{\mathrm{C}}=5000 \mathrm{psi}$ for the walls supporting the remaining slabs. Also, it is important to recognize that the displacements determined for Walls 2 and 3 are different than the expected values. The reason for this is because this calculation is assuming the wall is reacting to the force independently of all other walls. In actuality, however, Walls 4-7 serve as flanges for Walls 2 and 3, and will help to resist some of this movement. The above calculation was done solely as an approximation. To compute story drifts and displacements of shear walls working together by hand is beyond the scope of this technical assignment, and because of this the values therefore cannot be directly compared to the ETABS model.

## Overturning

Overturning moments are due to the presence of the lateral forces and can be found by multiplying the story forces by their mid-heights. This was done with the north/south wind forces and the east west seismic forces with values shown in Table 12. These moments are transformed into axial loads as they are transmitted through the lateral elements and into the 30 " mat slab foundation, which would experience the most impact from the overturning moment. To do a rough estimate of whether or not overturning would be an issue in 40 Bond, the stresses due to these lateral loads were examined and compared to the stresses due to the dead load (self weight) of the building which serves to counteract the overturning. Calculations supporting this estimate can be found in Appendix F. Because the stresses produced by the lateral forces are only a small fraction of that produced by the self weight of the structure, the overturning will have a minimal effect on the foundation. Due to the presence of the moments, however, it is expected that there will be a slight increase of force around the perimeter with a small uplift force on the windward sides and a slight downward force on the leeward sides.

| Table 12 - Overturning |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Floor | Height Above Ground-z (ft) | Story <br> Height (ft) | N/S Wind Forces |  | E/W Seismic Forces |  |
|  |  |  | Lateral Force $F_{x}(k)$ | $\begin{gathered} \text { Moment Total } \\ (\mathrm{ft}-\mathrm{k}) \end{gathered}$ | $\begin{gathered} \text { Lateral Force } \\ \mathrm{F}_{\mathrm{x}}(\mathrm{k}) \end{gathered}$ | Moments $\mathrm{M}_{\mathrm{x}}$ (ft-k) |
| PH Roof | 134.30 | 14.75 | 56.96 | 7227.76 | 10.86 | 1378.11 |
| PH | 119.55 | 12.66 | 67.58 | 7649.64 | 31.50 | 3566.31 |
| 10 | 106.89 | 11.83 | 62.31 | 6290.03 | 25.33 | 2556.85 |
| 9 | 95.06 | 11.83 | 61.48 | 5478.76 | 25.22 | 2247.37 |
| 8 | 83.23 | 11.83 | 60.37 | 4665.74 | 25.22 | 1949.01 |
| 7 | 71.40 | 12.58 | 63.02 | 4100.92 | 37.73 | 2455.33 |
| 6 | 58.82 | 11.83 | 57.88 | 3059.54 | 36.55 | 1931.96 |
| 5 | 46.99 | 11.83 | 56.22 | 2306.59 | 36.36 | 1491.67 |
| 4 | 35.16 | 11.83 | 54.55 | 1592.98 | 36.66 | 1070.44 |
| 3 | 23.33 | 10.83 | 47.91 | 856.20 | 39.99 | 714.69 |
| 2 | 12.50 | 12.5 | 52.96 | 330.99 | 35.69 | 223.09 |
| 1 | 0 | 0 | 0.00 | 0.00 | 4.58 | 0.00 |
|  |  | Total: | 641.25 | 43559.14 | 345.70 | 19584.83 |

## Conclusion

Once adjusting the values found in the first technical assignment, the lateral forces were applied to 40 Bond. These loads were then factored according to ASCE 7-05 load combinations for strength design. With output taken from ETABS, it was determined that the combination of $1.2 D+1.6 W+L+0.5\left(L_{r}\right.$ or $S$ or $\left.R\right)$ controlled in the north/south direction, while $0.9 D+$ $1.0 E+1.6 \mathrm{H}$ controlled in the east/west direction. A reason for wind controlling in one direction and seismic controlling in the other is most likely due to the large surface area of the north and south facades. This area, which is more than twice as large as the east and west faces, resulted in larger wind forces in that direction.

Although ETABS was used as a reference and in some comparisons to verify that the model and hand calculations were providing similar and reasonable results, the values computed by hand were those used in all subsequent calculations. There were two reasons behind this. First, it was concluded after finding the center of rigidity that the model was taking the slab into account as a member providing lateral resistance rather than acting as a null diaphragm. Secondly, because this was the first encounter using ETABS to model a structure, there was some uncertainty as to whether or not everything was input with all the proper assumptions. Therefore, to ensure consistency and to verify that only the shear walls were acting to resist lateral forces, hand calculations were done. Anything that was beyond the scope of hand calculations was taken from the ETABS model.

This report confirms that looking to the shear walls alone was a reasonable assumption. There was torsion due to the eccentricity between the center of mass and the center of rigidity that added torsional shear to the walls. Shear strength checks were done including both the direct and torsional shear and it was deduced that the thickness, length and reinforcement were designed to adequately resist the total shear. Overall building drift, as determined by ETABS output, was within the limit of $\mathrm{H} / 400$. The story drifts and displacements that were calculated by hand were within a reasonable range, but they neglected the effect of the core working as one unit. Because of this the values are only an approximation and are most likely smaller. Overturning is present due to the lateral loads, but a stress check concluded that the self weight of the building can do most of the work to resist this. A more complex model and additional calculations will follow when the second portion of senior thesis begins. At this stage of analysis, however, it was determined that the shear walls were satisfactorily designed to resist various combinations of loading.

# Appendix A <br> Shear Wall Elevations 

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Figure 12- Elevation of Wall 1


Figure 13- Elevation of Wall 2


Figure 14- Elevation of Wall 3


Figure 15 - Elevation of Walls 4 and 5


Figure 16 - Elevation of Walls 6 and 7

## Appendix B

## Loads

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## Wind Loads

| Table 13 - Wind Loads (North/South Direction) B=134'-4", L=64'-8" |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Floor | Height <br> Above Ground-z <br> (ft) | Story Height (ft) | $\mathrm{K}_{\mathrm{z}}$ | $\mathrm{q}_{\mathrm{z}}$ | Wind Pres | ssure (psf) Leeward | Total Pressure (psf) | Force (k) of Windward Only | Force (k) of Total Pressure | Story <br> Shear Windward (k) | Story <br> Shear <br> Total (k) | Moment Windward (ft-k) | Moment <br> Total (ft-k) |
| PH Roof | 134.30 | 14.75 | 1.08 | 28.44 | 23.86 | -16.57 | 40.43 | 33.61 | 56.96 | 33.61 | 56.96 | 4265.08 | 7227.76 |
| PH | 119.55 | 12.66 | 1.04 | 27.38 | 23.16 | -16.57 | 39.74 | 39.39 | 67.58 | 73.00 | 124.53 | 4458.98 | 7649.64 |
| 10 | 106.89 | 11.83 | 1.01 | 26.59 | 22.64 | -16.57 | 39.21 | 35.98 | 62.31 | 108.98 | 186.85 | 3631.46 | 6290.03 |
| 9 | 95.06 | 11.83 | 0.98 | 25.80 | 22.12 | -16.57 | 38.69 | 35.14 | 61.48 | 144.12 | 248.33 | 3131.76 | 5478.76 |
| 8 | 83.23 | 11.83 | 0.94 | 24.75 | 21.42 | -16.57 | 37.99 | 34.04 | 60.37 | 178.16 | 308.70 | 2630.33 | 4665.74 |
| 7 | 71.40 | 12.58 | 0.9 | 23.70 | 20.72 | -16.57 | 37.29 | 35.02 | 63.02 | 213.17 | 371.73 | 2278.44 | 4100.92 |
| 6 | 58.82 | 11.83 | 0.85 | 22.38 | 19.85 | -16.57 | 36.42 | 31.54 | 57.88 | 244.71 | 429.61 | 1667.31 | 3059.54 |
| 5 | 46.99 | 11.83 | 0.79 | 20.80 | 18.80 | -16.57 | 35.38 | 29.88 | 56.22 | 274.59 | 485.83 | 1225.93 | 2306.59 |
| 4 | 35.16 | 11.83 | 0.73 | 19.22 | 17.76 | -16.57 | 34.33 | 28.22 | 54.55 | 302.81 | 540.38 | 823.91 | 1592.98 |
| 3 | 23.33 | 10.83 | 0.65 | 17.11 | 16.36 | -16.57 | 32.93 | 23.80 | 47.91 | 326.61 | 588.29 | 425.33 | 856.20 |
| 2 | 12.50 | 12.5 | 0.57 | 15.01 | 14.97 | -16.57 | 31.54 | 25.13 | 52.96 | 351.74 | 641.25 | 157.05 | 330.99 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 351.74 | 641.25 | 0.00 | 0.00 |
| $\Sigma$ Story S <br> (Windwa |  | 351.74 k | $\Sigma$ Story <br> (Total) | Shear | 641.25 k | $\Sigma$ Moment (Windward) $=$ |  | $24695.58 \mathrm{ft}-\mathrm{k}$ |  | $\Sigma$ Moment (Total) = |  | $43559.14 \mathrm{ft}-\mathrm{k}$ |  |
| $\Sigma$ DCE Story Shear (Windward) $=360 \mathrm{k}$ |  |  |  |  |  | $\Sigma$ DCE Moment (Windward) $=30200 \mathrm{ft}-\mathrm{k}$ |  |  |  |  |  |  |  |





## Seismic Loads

| Table 15 - Seismic Loads (ASCE 7-05) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Level | Story Weight $\mathbf{w}_{\mathrm{x}}$ (kips) | Height $\mathrm{h}_{\mathrm{x}}(\mathbf{f t}$ ) | $h_{x}{ }^{\text {k }}$ | $\mathrm{w}_{\mathrm{x}} \mathrm{h}_{\mathrm{x}}{ }^{\text {k }}$ | $\mathrm{C}_{\mathrm{vx}}$ | Lateral <br> Force $\mathbf{F}_{\mathbf{x}}$ | Story Shear $\mathbf{V}_{\mathrm{x}}$ (kips) | Moments $\mathbf{M}_{\mathrm{x}}(\mathrm{ft}-\mathrm{k})$ |
| PH Roof | 394.00 | 134.30 | 266.69 | 105075.84 | 0.07 | 10.97 | 0.00 | 1392.20 |
| PH | 1143.00 | 119.55 | 233.56 | 266964.03 | 0.19 | 27.87 | 10.97 | 3155.28 |
| 10 | 919.00 | 106.89 | 205.58 | 188931.24 | 0.13 | 19.73 | 38.84 | 1991.16 |
| 9 | 915.00 | 95.06 | 179.85 | 164565.43 | 0.11 | 17.18 | 58.57 | 1531.10 |
| 8 | 915.00 | 83.23 | 154.57 | 141429.55 | 0.10 | 14.77 | 75.75 | 1141.16 |
| 7 | 1369.00 | 71.40 | 129.78 | 177672.17 | 0.12 | 18.55 | 90.52 | 1207.09 |
| 6 | 1326.00 | 58.82 | 104.05 | 137975.52 | 0.10 | 14.41 | 109.07 | 761.50 |
| 5 | 1319.00 | 46.99 | 80.55 | 106250.50 | 0.07 | 11.09 | 123.48 | 455.17 |
| 4 | 1330.00 | 35.16 | 57.88 | 76974.58 | 0.05 | 8.04 | 134.57 | 234.68 |
| 3 | 1451.00 | 23.33 | 36.26 | 52612.65 | 0.04 | 5.49 | 142.61 | 98.16 |
| 2 | 1295.00 | 12.50 | 17.80 | 23054.05 | 0.02 | 2.41 | 148.10 | 15.04 |
| 1* | 166.20 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 150.51 | 0.00 |
| $\Sigma \mathrm{w}_{\mathrm{i}} \mathrm{h}_{\mathrm{i}}{ }^{\text {k }}$ | 1441505.58 | $\Sigma \mathrm{F}_{\mathrm{x}}=\mathrm{V}_{\mathrm{x}}=$ | 150.5064 k |  |  | ments $\mathrm{M}_{\mathrm{x}}=$ | 11982.54 |  |
| Total Building Weight (Above Grade) |  |  | 12542.20 k |  |  |  |  |  |
| * First floor story weight is only the weight of the columns whose base is at the ground floor. Weights of slab, beams and superimposed dead load on the ground floor are not considered because base shear is related to levels above grade and those components mentioned are at grade. |  |  |  |  |  |  |  |  |

Table 16 - Seismic Loads (NYCBC)

| Level | Story Weight $\mathrm{w}_{\mathrm{x}}$ (kips) | Height $\mathbf{h}_{\mathbf{x}}(\mathbf{f t})$ | (ZIC/R ${ }_{\text {w }}$ ) | Lateral <br> Force $\mathrm{F}_{\mathrm{x}}$ | Story Shear $\mathbf{V}_{\mathrm{x}}$ (kips) | Moments $\mathbf{M}_{x}(f t-k)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PH Roof | 394.00 | 134.30 | 0.02756 | 10.86 | 0.00 | 1378.11 |
| PH | 1143.00 | 119.55 | 0.02756 | 31.50 | 10.86 | 3566.31 |
| 10 | 919.00 | 106.89 | 0.02756 | 25.33 | 42.36 | 2556.85 |
| 9 | 915.00 | 95.06 | 0.02756 | 25.22 | 67.69 | 2247.37 |
| 8 | 915.00 | 83.23 | 0.02756 | 25.22 | 92.91 | 1949.01 |
| 7 | 1369.00 | 71.40 | 0.02756 | 37.73 | 118.14 | 2455.33 |
| 6 | 1326.00 | 58.82 | 0.02756 | 36.55 | 155.87 | 1931.96 |
| 5 | 1319.00 | 46.99 | 0.02756 | 36.36 | 192.42 | 1491.67 |
| 4 | 1330.00 | 35.16 | 0.02756 | 36.66 | 228.77 | 1070.44 |
| 3 | 1451.00 | 23.33 | 0.02756 | 39.99 | 265.43 | 714.69 |
| 2 | 1295.00 | 12.50 | 0.02756 | 35.69 | 305.43 | 223.09 |
| 1* | 166.20 | 0.00 | 0.02756 | 4.58 | 341.12 | 0.00 |
| $\Sigma \mathrm{F}_{\mathrm{x}}=\mathrm{V}_{\mathrm{x}}=$ | 345.70 |  |  | oments $\mathrm{M}_{\mathrm{x}}=$ | 19584.83 |  |

Total Building Weight (Above Grade)
12542.20 k

* First floor story weight is only the weight of the columns whose base is at the ground floor. Weights of slab, beams and superimposed dead load on the ground floor are not considered because base shear is related to levels above grade and those components mentioned are at grade.



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## Appendix C

Load Distribution

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## Rigidity, Relative Stiffness, and Center of Rigidity

| Table 17 - Wall Rigidity Calculation (N-S Span) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Supported Floor | Ht | Wall 1 | Wall 2 | Wall 3 | $\Sigma$ Rigidities | Center of Rigidity (x) |
|  |  | Length - 256" | Length - 323" | Length - 323" |  |  |
| Floor 1 | 150 | 23874 | 34104 | 34104 | 92082 | 706.4 |
| Floor 2 | 280 | 7184 | 11750 | 11750 | 30685 | 730.1 |
| Floor 3 | 422 | 2676 | 4764 | 4764 | 12205 | 744.2 |
| Floor 4 | 564 | 979 | 1823 | 1823 | 4624 | 751.3 |
| Floor 5 | 706 | 525 | 1001 | 1001 | 2526 | 755.1 |
| Floor 6 | 857 | 302 | 585 | 585 | 1472 | 757.5 |
| Floor 7* | 999 | 144 | 379 | 379 | 902 | 800.8 |
| Floor 8* | 1141 | 74 | 259 | 259 | 591 | 833.9 |
| Floor 9* | 1283 | 40 | 184 | 184 | 409 | 857.9 |
| Floor 10* | 1435 | 23 | 133 | 133 | 288 | 876.7 |
| Penthouse* | 1612 | 0 | 74 | 74 | 147 | 951.5 |


| Table 18 -Wall Rigidity Calculation (E-W Span) |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ht | Wall 4 | Wall 5 | Wall 6 | Wall 7 | $\Sigma$ Rigidities | Center of Rigidity (y) |
|  |  | Length - 122" | Length - 90.5" | Length - 99" | Length - 90.5" |  |  |
| Floor 1* | 150 | 5500 | 2639 | 8 | 328 | 8474 | 642.2 |
| Floor 2 | 280 | 1107 | 479 | 442 | 160 | 2189 | 566.1 |
| Floor 3 | 422 | 348 | 146 | 158 | 77 | 729 | 550.7 |
| Floor 4 | 564 | 118 | 49 | 57 | 32 | 255 | 543.5 |
| Floor 5 | 706 | 61 | 25 | 30 | 18 | 134 | 539.4 |
| Floor 6 | 857 | 34 | 14 | 17 | 11 | 77 | 536.0 |
| Floor 7 | 999 | 22 | 9 | 11 | 7 | 49 | 535.1 |
| Floor 8 | 1141 | 15 | 6 | 7 | 5 | 33 | 534.1 |
| Floor 9 | 1283 | 10 | 4 | 5 | 4 | 23 | 533.0 |
| Floor 10 | 1435 | 7 | 3 | 4 | 3 | 17 | 530.6 |
| Penthouse | 1612 | 0 | 2 | 0 | 0 | 2 | 655.0 |




## Appendix D

## Shear

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## Appendix E

Drift and Displacement
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| Table 19 - Wall 1 Displacement Calculations |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Supported Floor | Lateral <br> Force (k) | $\mathrm{E}_{\mathrm{c}} \quad(\mathrm{ksi})$ | $\begin{gathered} \mathrm{E}_{\mathrm{r}} \\ (\mathrm{ksi}) \end{gathered}$ | Thickness <br> (in) | Length (in) | Height <br> (in) | $\Delta_{\text {flexural }}$ (in) | $\begin{gathered} \Delta_{\text {shear }} \\ \text { (in) } \end{gathered}$ | Story Displacement (in) | Story Drift (in) |
| Floor 2 | 14.77 | $5.10 \mathrm{E}+03$ | $2.04 \mathrm{E}+03$ | 12 | 256 | 150 | 0.000194 | 0.000424 | 0.00062 | 4.1236E-06 |
| Floor 3 | 15.82 | $5.10 \mathrm{E}+03$ | $2.04 \mathrm{E}+03$ | 12 | 256 | 280 | 0.001354 | 0.000849 | 0.00220 | 7.86519E-06 |
| Floor 4 | 13.66 | $5.10 \mathrm{E}+03$ | $2.04 \mathrm{E}+03$ | 12 | 256 | 422 | 0.004001 | 0.001104 | 0.00511 | $1.2099 \mathrm{E}-05$ |
| Floor 5 | 13.02 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 256 | 564 | 0.011516 | 0.001779 | 0.01330 | $2.35732 \mathrm{E}-05$ |
| Floor 6 | 12.54 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 256 | 706 | 0.021756 | 0.002145 | 0.02390 | $3.38542 \mathrm{E}-05$ |
| Floor 7 | 12.93 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 256 | 857 | 0.04013 | 0.002686 | 0.04282 | $4.99601 \mathrm{E}-05$ |
| Floor 8 | 9.23 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 231 | 999 | 0.061724 | 0.002475 | 0.06420 | $6.42637 \mathrm{E}-05$ |
| Floor 9 | 6.99 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 210 | 1141 | 0.092774 | 0.002357 | 0.09513 | $8.33748 \mathrm{E}-05$ |
| Floor 10 | 5.40 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 192.8 | 1283 | 0.131638 | 0.002229 | 0.13387 | 0.000104339 |
| Penthouse | 3.79 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 178 | 1435 | 0.164203 | 0.001895 | 0.16610 | 0.000115747 |
| Penthouse Roof | 0.00 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 0 | 1612 | 0 | 0 | 0.00000 | 0 |
| Total Wall Displacement (in) $=0.54723$ |  |  |  |  |  |  |  |  |  |  |


| Table 20 - Wall 2 \& 3 Displacement Calculations |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Supported Floor | Lateral <br> Force (k) | $\mathrm{E}_{\mathrm{C}} \quad(\mathrm{ksi})$ | $\begin{gathered} \mathrm{E}_{\mathrm{r}} \\ (\mathrm{ksi}) \end{gathered}$ | t (in) | Length <br> (in) | Height <br> (in) | $\Delta_{\text {flexural }}$ (in) | $\Delta_{\text {shear }}$ <br> (in) | Story <br> Displacement <br> (in) | Story Drift (in) |
| Floor 2 | 21.09 | $5.10 \mathrm{E}+03$ | $2.04 \mathrm{E}+03$ | 12 | 323 | 150 | 0.000138 | 0.00048 | 0.00062 | $4.94832 \mathrm{E}-05$ |
| Floor 3 | 25.88 | $5.10 \mathrm{E}+03$ | $2.04 \mathrm{E}+03$ | 12 | 323 | 280 | 0.001102 | 0.0011 | 0.00220 | 7.86519E-06 |
| Floor 4 | 24.33 | $5.10 \mathrm{E}+03$ | $2.04 \mathrm{E}+03$ | 12 | 323 | 422 | 0.003547 | 0.001559 | 0.00511 | $1.2099 \mathrm{E}-05$ |
| Floor 5 | 24.23 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 323 | 564 | 0.010671 | 0.002625 | 0.01330 | $2.35732 \mathrm{E}-05$ |
| Floor 6 | 23.92 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 323 | 706 | 0.020658 | 0.003243 | 0.02390 | $3.38542 \mathrm{E}-05$ |
| Floor 7 | 25.05 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 323 | 857 | 0.038693 | 0.004122 | 0.04282 | $4.99601 \mathrm{E}-05$ |
| Floor 8 | 24.33 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 323 | 999 | 0.059532 | 0.004668 | 0.06420 | $6.42637 \mathrm{E}-05$ |
| Floor 9 | 24.61 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 323 | 1141 | 0.089737 | 0.005393 | 0.09513 | $8.33748 \mathrm{E}-05$ |
| Floor 10 | 24.58 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 323 | 1283 | 0.1274 | 0.006056 | 0.13346 | 0.000104019 |
| Penthouse | 22.06 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 323 | 1435 | 0.160017 | 0.00608 | 0.16610 | 0.000115747 |
| Penthouse Roof | 26.48 | $4.03 \mathrm{E}+03$ | $1.61 \mathrm{E}+03$ | 12 | 297 | 1612 | 0 | 0 | 0 | 0 |
| Total wall displacement (in) $=0.54682$ |  |  |  |  |  |  |  |  |  |  |






## Appendix F <br> Overturning

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